

# BIOPHARMACY

## Pharmacokinetics -2-

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Data: Dose = 400 mg,  $C_p$ 2hr = 4.5 mg/L,  $C_p$ 6hr = 3.7 mg/L

- Question: k and V?
- Equation:  $k = (\ln C_{p1} - \ln C_{p2}) / t_2 - t_1$

$$k = (\ln(4.5) - \ln(3.7)) / (6 - 2) = 0.049 \text{ hr}^{-1}$$

$$\ln C_p = \ln C_p^0 - kt$$

$$\ln C_p^0 = \ln(4.5) + 0.049 \times 2 = 1.602$$

$$C_p^0 = 4.96$$

$$V = \text{Dose} / C_p^0 = 400 / 4.96 = 80.6 \text{ L}$$

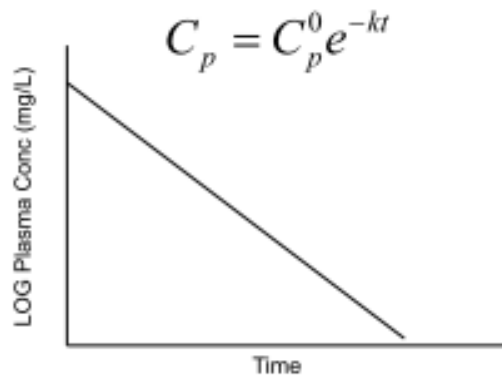
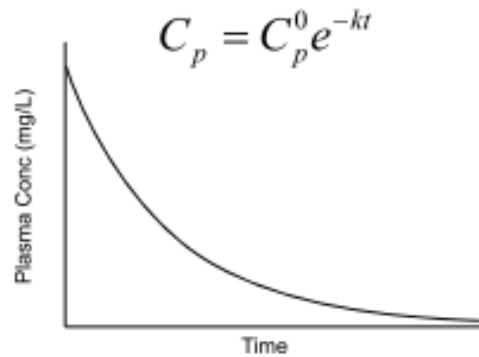
# Two Compartment Model – IV

## One Compartment

No absorption

Instantaneous Distribution

Elimination phase

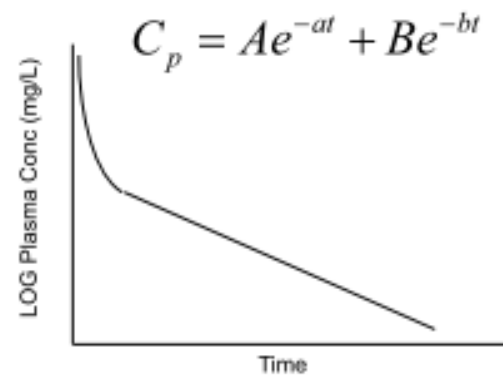
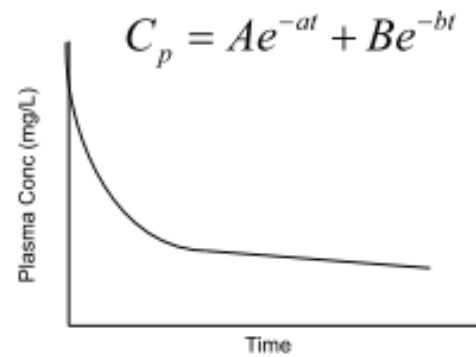


## Two Compartment

No absorption

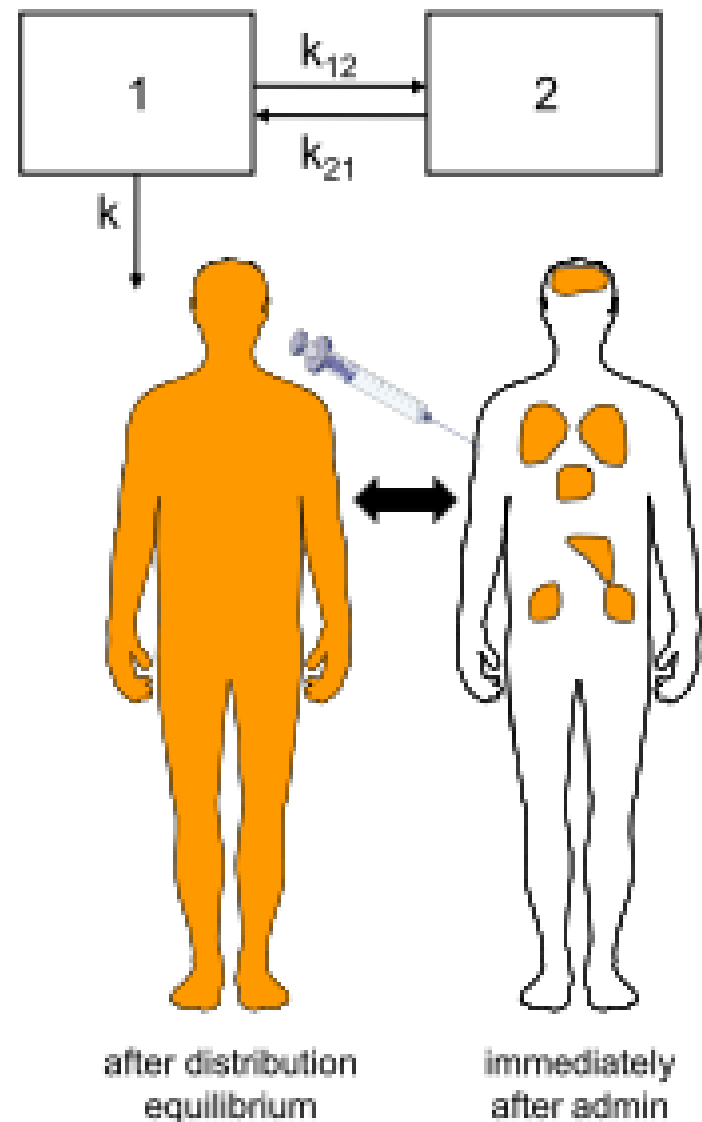
Distribution phase

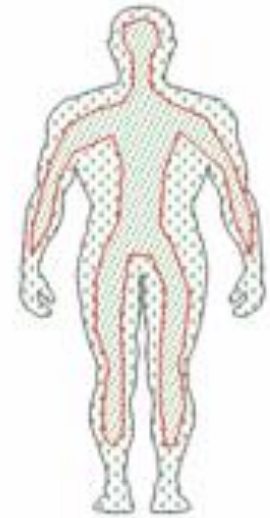
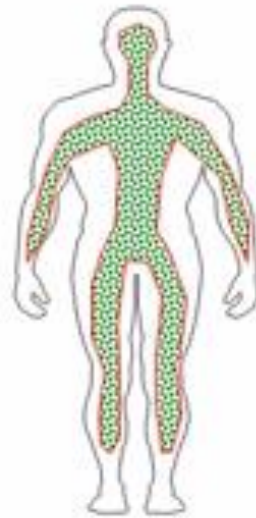
Elimination phase



## Two Compartment Model - IV

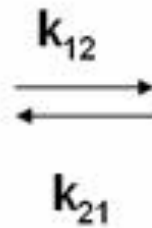
- IV administration
  - no absorption
  - immediate distribution to rapidly perfused organs “central compartment”
  - subsequent distribution into slowly perfused organs “peripheral compartment”
- Assumes all transfer rates are **first-order** processes
- Tissue uptake depends on lipophilicity, ionization, protein binding





**Before distribution**

**After distribution**



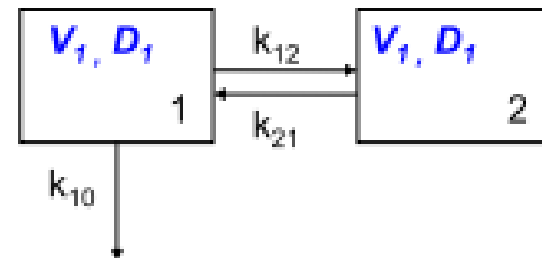
$k$

**$A_1$  = central compartment**

**$A_2$  = peripheral compartment**

## Two Compartment Model - IV

- What are the PK parameters to define a 2 compartment model?
- Micro rate constants
  - $k_{12}$ ,  $k_{21}$ ,  $k_{10}$
- Simpler to use biexponential equation
  - $a$  and  $b$  are hybrid rate constants
  - $a + b = k_{12} + k_{21} + k_{10}$
  - $a =$  distribution rate constant
  - $b =$  elimination rate constant
  - $A$  and  $B$  are intercepts on the y-axis



$$C_p = Ae^{-at} + Be^{-bt}$$

## Determination of A, a, B and b

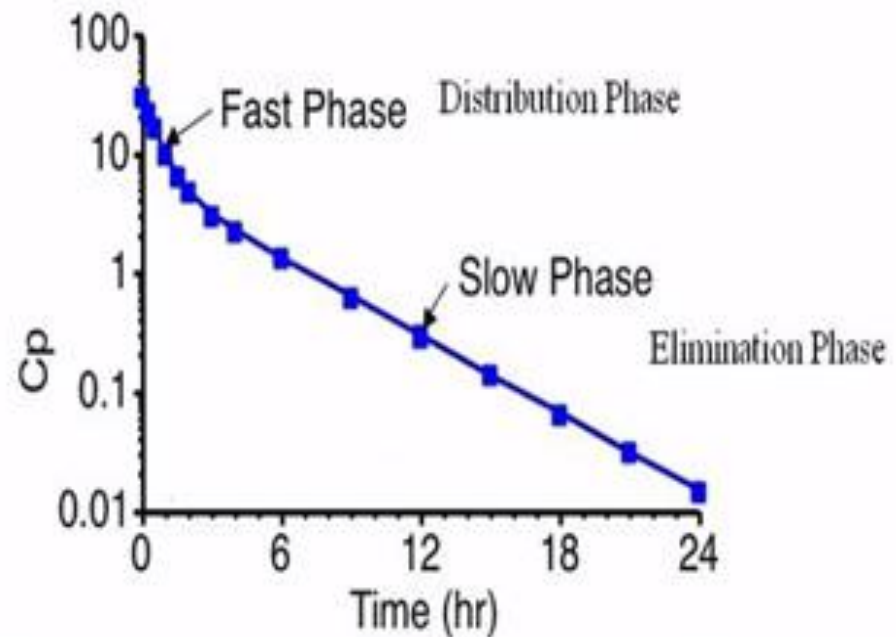
- To calculate values for A and a we need to separate distribution phase from the elimination phase

$$C_p = Ae^{-at} + Be^{-bt}$$

$$\therefore Ae^{-at} = C_p - Be^{-bt}$$

- A is determined from the slope of the 'stripped' curve and a is calculated from the gradient

Plasma concentration time curve for a drug that follows a two compartment model shows that the plasma drug concentration declines bi-exponentially as the sum of two first order processes: **distribution and elimination**



In this model, the drug distributes into two compartments, the **central** compartment (plasma & highly perfused tissues) and the **tissue or peripheral** compartment.

The distribution phase may take minutes or hours, and may be missed if plasma samples were taken too late or at wide intervals after the injection.



## Plasma Concentration time curve

Distribution Phase

Elimination Phase

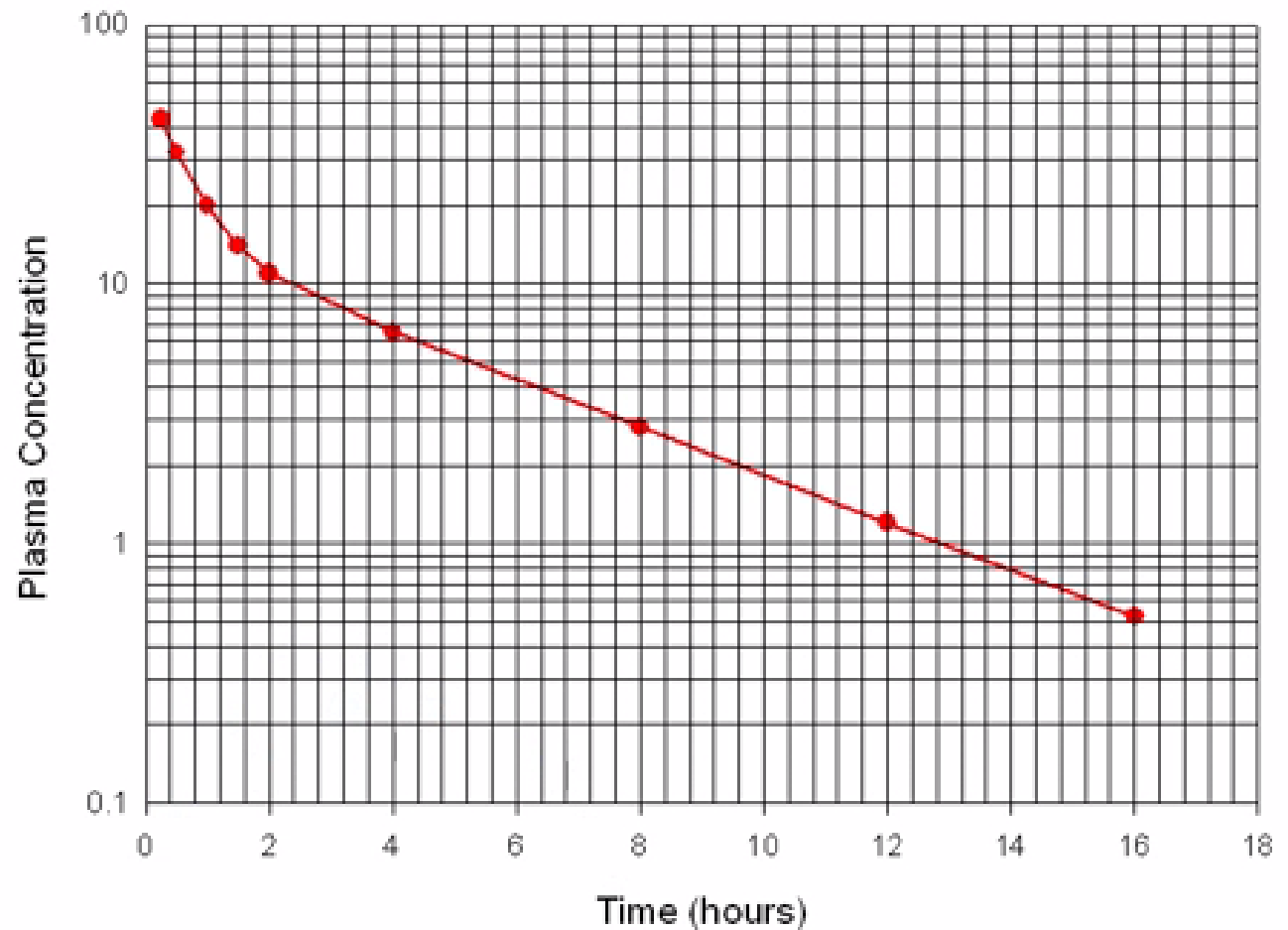
At first, initial rapid decline in drug concentration due to rapid transfer from central to peripheral compartment

Drug in central compartment  $\equiv$  Drug in peripheral compartment

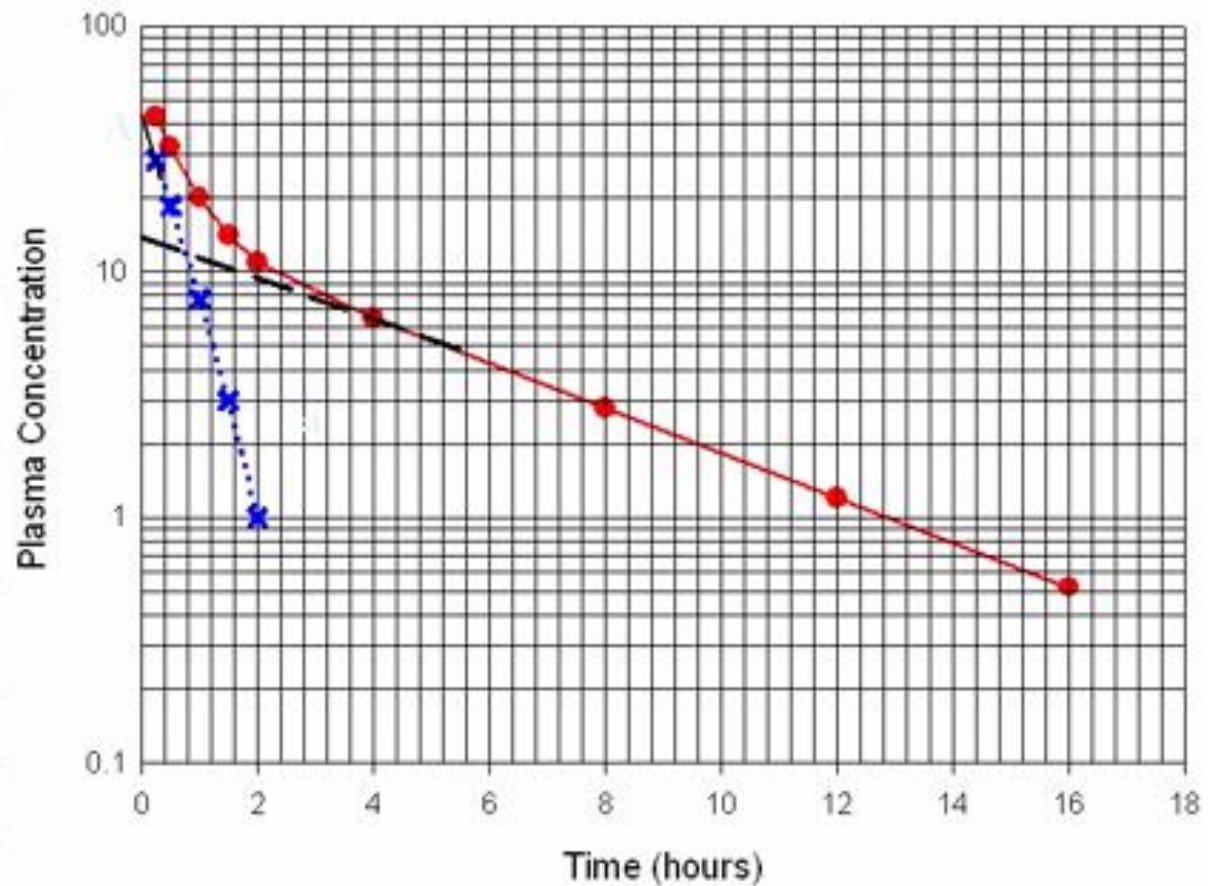
Drug declines in both central and peripheral compartment following first order process

## Method of Residuals (Feathering Method)

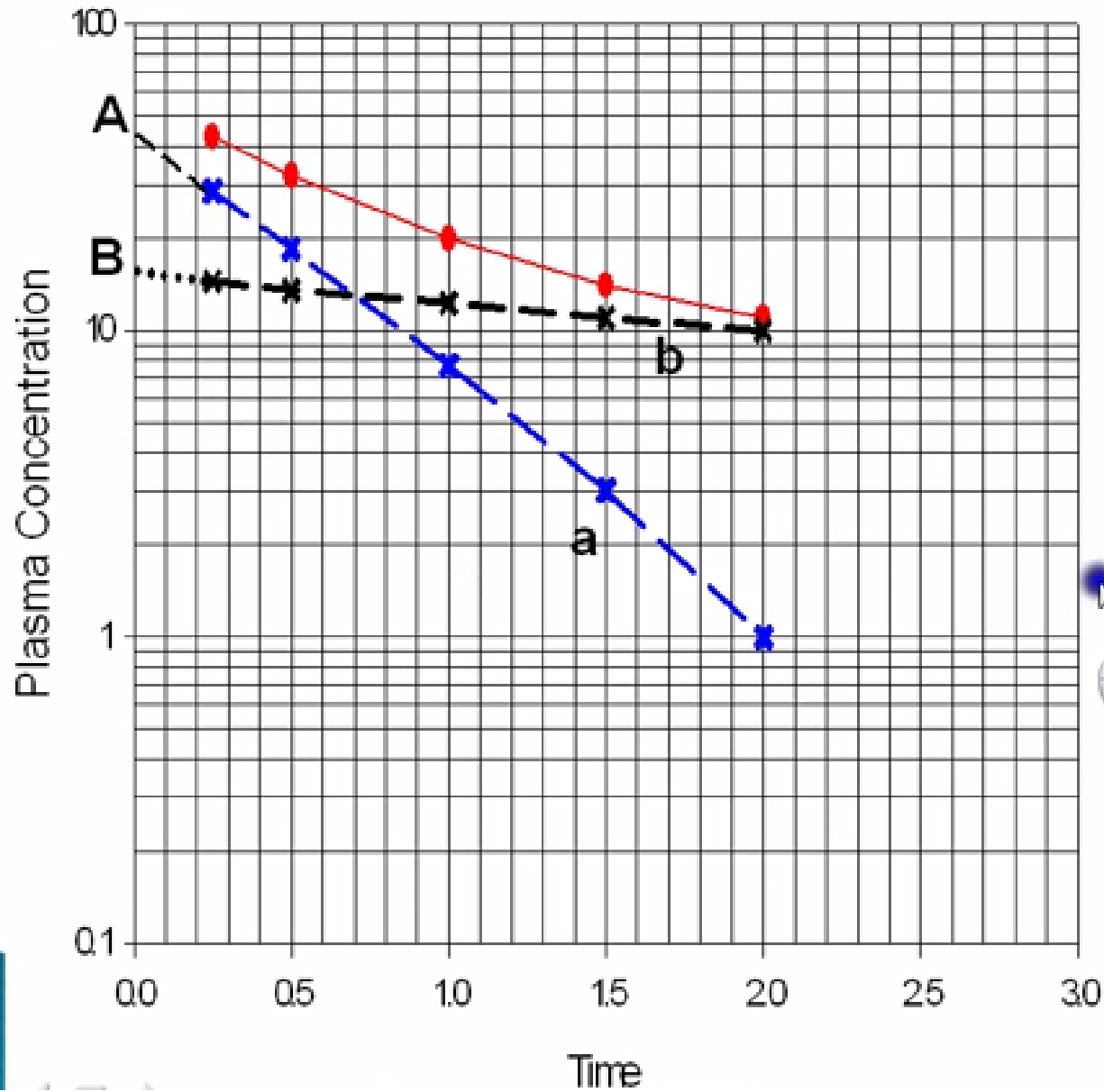
Time	C <sub>p</sub>
0.25	43
0.5	32
1	20
1.5	14
2	11
4	6.5
8	2.8
12	1.2
16	0.52



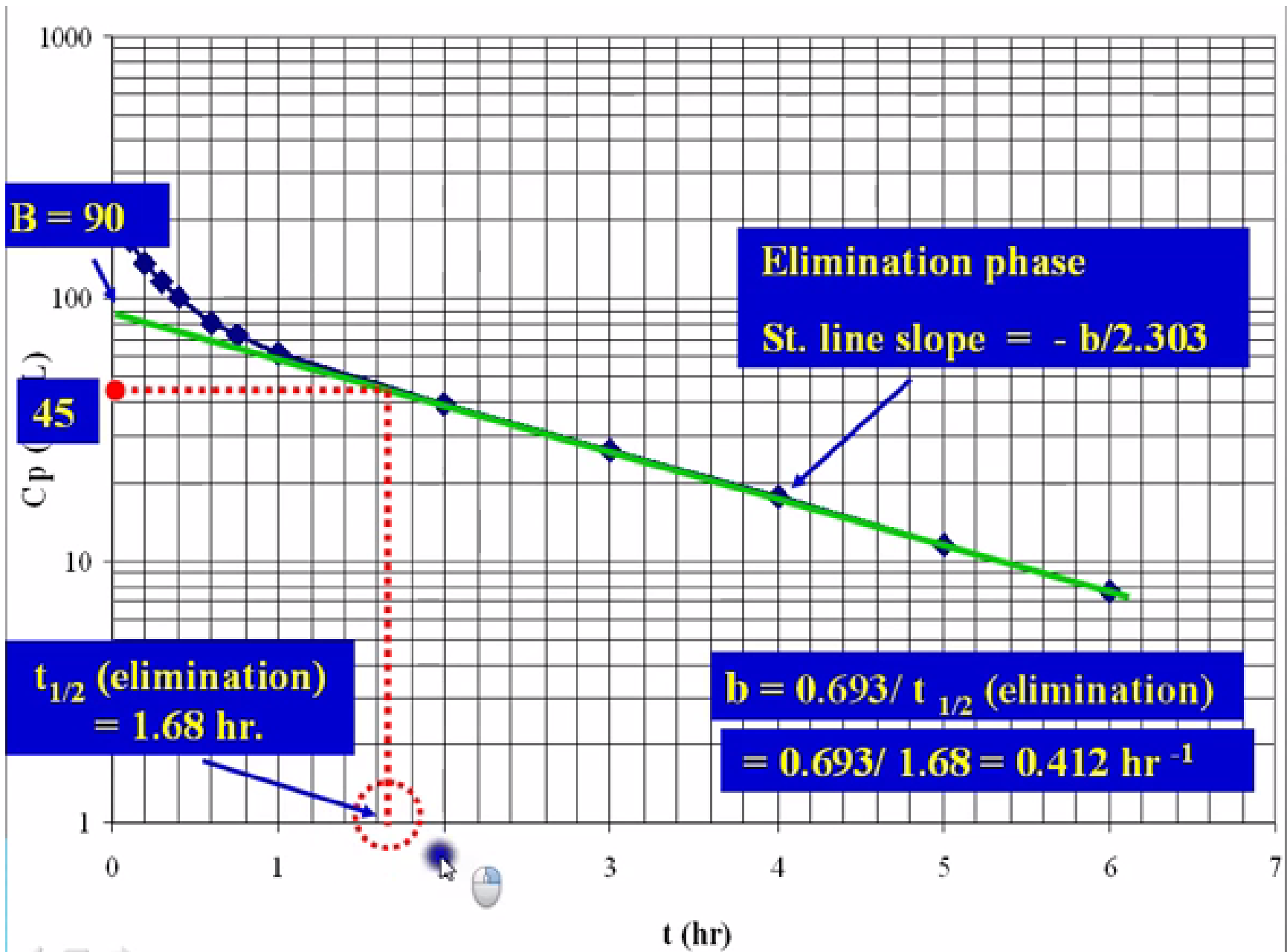
Time	Cp	Cp'	Cp-Cp'
0.25	43	14.5	43-14.5 = 28.5
0.5	32	13.5	32-13.5 = 18.5
1	20	12.3	20-12.3 = 7.7
1.5	14	11	14-11 = 3.0
2	11	10	11-10 = 1.0
4	6.5		
8	2.8		
12	1.2		
16	0.52		



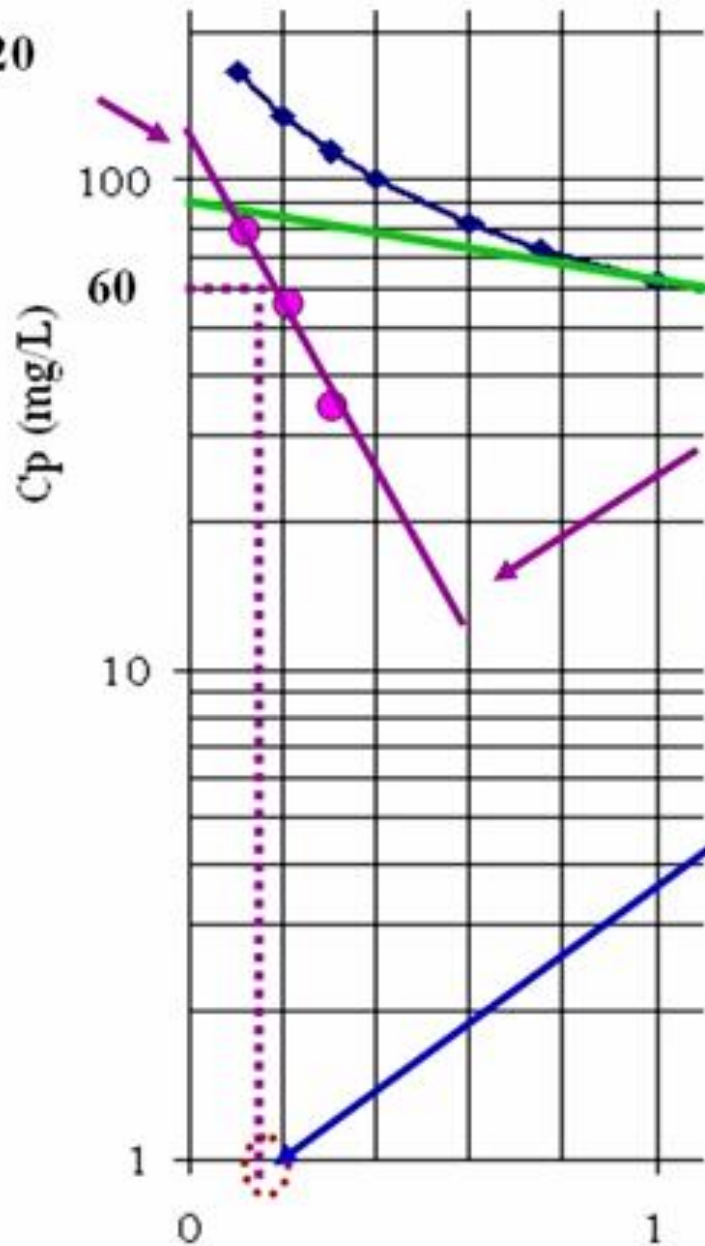
a or  $\alpha$  phase



Time	Cp-Cp'
<b>0.25</b>	<b>43-14.5 = 28.5</b>
<b>0.5</b>	<b>32-13.5 = 18.5</b>
<b>1</b>	<b>20-12.3 = 7.7</b>
<b>1.5</b>	<b>14.-11 = 3.0</b>
<b>2</b>	<b>11-10 = 1.0</b>



$A = 120$



Residual line  
St. line of distribution  
Slope =  $-a / 2.303$

$$t_{1/2} = 0.693 / a \text{ (distribution)}$$

$$t_{1/2} \text{ (distribution)} = 0.18 \text{ hr.}$$



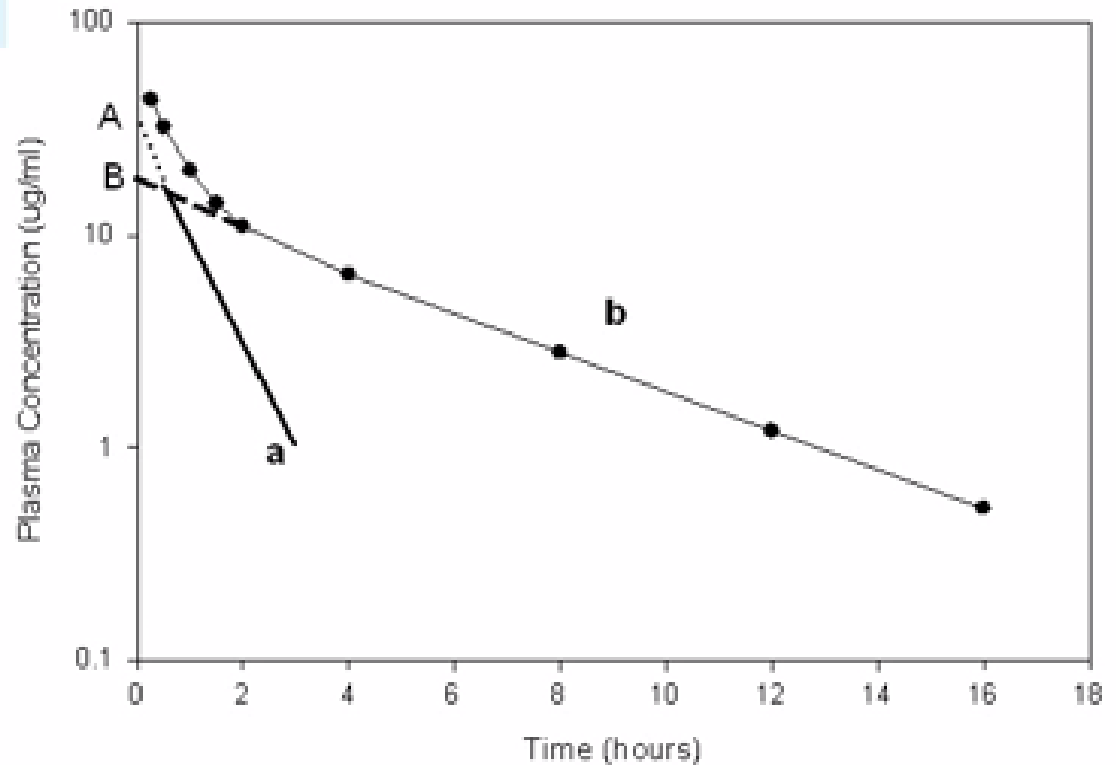
$$C_p = A e^{-at} + B e^{-bt}$$

$$a + b = k_{12} + k_{21} + k$$

$$ab = k_{21}k$$

$$A = \frac{D^0 (a - k_{21})}{V_p (a - b)}$$

$$B = \frac{D^0 (k_{21} - b)}{V_p (a - b)}$$



The decline in the initial distribution phase is more rapid than the elimination phase.  
 The rapid distribution is confirmed by the constant  $a$  being larger than the rate constant  $b$ .

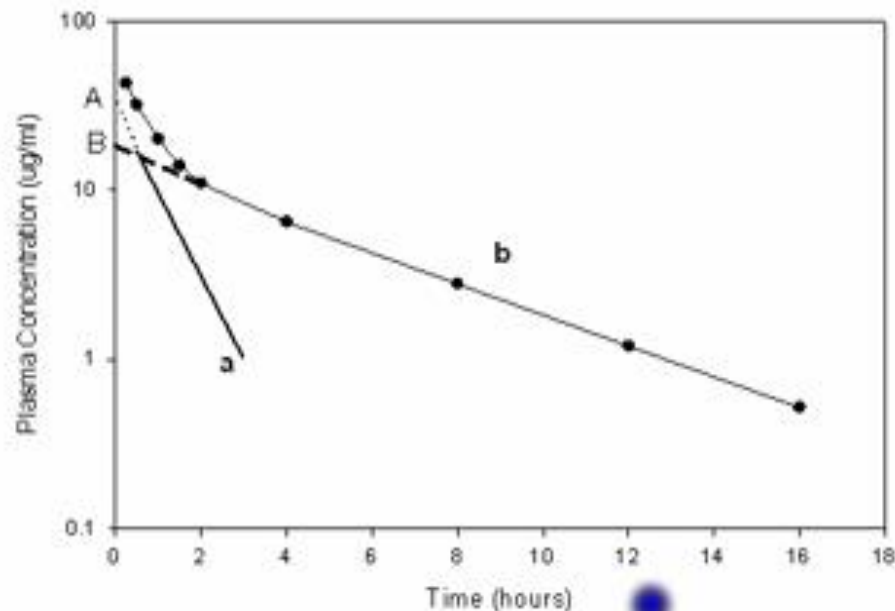
$$C_p = B e^{-bt}$$

$$\log C_p = \frac{-bt}{2.303} + \log B$$

Rate constant can be obtained from the slope =  $(-b/2.3)$

Terminal elimination half-life equals to

$$t_{1/2} = \frac{0.693}{b}$$





## Apparent Volumes of Distribution

$$C_p = A e^{-at} + B e^{-bt}$$

At  $t=0$ ,  $e^0 = 1$  therefore

$$C_p^0 = A+B$$

$V_p$  is determined by determining  $A$  and  $B$  from the residual line.

$$V_p = \frac{D^0}{A+B}$$

## Elimination rate constant:

- The elimination rate constant **k** represents the elimination of drug from the central compartment.
- **b** represents drug elimination during the elimination phase only, when distribution is mostly complete.
- Therefore **b** is smaller than **k**, where **k** is the true elimination constant.
- While **b** is a hybrid constant that is affected by the rate of drug transfer in and out of the tissue compartment


$$a > b, \quad b < k$$

## Determination of Compartment Models:

The observed number of compartments will depend on:

- 1- The route of drug administration.
- 2- Sampling intervals (missed compartment if later than distribution phase)
- 3- The number of samples taken during the collection period (depend on  $t_{1/2}$ ).
- 4- The assay sensitivity (lower drug concentrations could be missed).